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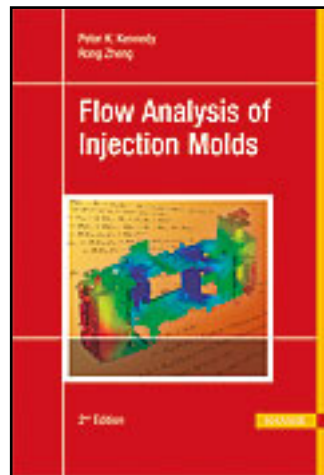


Table of Contents

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Flow Analysis of Injection Molds

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Contents

Preface	IX
Notation	XXI
I The Current Status of Simulation	1
1 Introduction	3
1.1 The Injection Molding Process	3
1.2 Molding Terminology	4
1.3 What is Simulation?	5
1.4 The Challenges for Simulation	6
1.4.1 Basic Physics of the Process	7
1.5 Why Simulate Injection Molding?	7
1.6 How Good is Simulation?	8
2 Stress and Strain in Fluid Mechanics	11
2.1 Stress in Fluids	11
2.1.1 The Stress Tensor	11
2.1.2 The Extra Stress Tensor	14
2.1.3 Rate of Strain Tensor	14
2.2 Newtonian and Non-Newtonian Fluids	15
2.3 The Generalized Newtonian Fluid	16
3 Material Properties of Polymers	19
3.1 Types of Polymers	19
3.2 Amorphous Polymers	20
3.3 Semi-Crystalline Polymers	20
3.4 Overview of Material Properties for Simulation	21
3.5 Viscosity	22
3.6 Modeling Viscosity	23
3.6.1 The Viscosity Function	23

3.6.2	The Power Law Model	23
3.6.3	The Carreau Model	23
3.6.4	The Cross Model	24
3.6.5	Incorporation of Temperature Effects	24
3.6.6	The Solidification Problem	25
3.7	Thermal Properties	26
3.7.1	Specific Heat Capacity	26
3.7.2	Thermal Conductivity	27
3.8	Thermodynamic Relationships	29
3.8.1	Expansivity and Compressibility	29
3.9	Pressure-Volume-Temperature (PVT) Data	31
3.10	Fiber Orientation	31
3.11	Shrinkage and Warpage.....	32

4 Governing Equations..... 35

4.1	Introduction	35
4.2	Mathematical Preliminaries	35
4.2.1	The Material Derivative	35
4.2.2	The Gauss Divergence Theorem	36
4.2.3	Reynolds Transport Theorem	37
4.2.4	Integration by Parts	37
4.3	Conservation of Mass	38
4.4	Conservation of Momentum	38
4.5	Conservation of Energy	40
4.5.1	Relating Specific Energy to Temperature	43
4.5.2	The Energy Equation in Terms of Temperature	45
4.6	Boundary Conditions	46
4.6.1	Pressure and Flow Rate Boundary Conditions.....	47
4.6.2	Temperature Boundary Conditions	48
4.6.3	Mold Deformation Boundary Conditions	48
4.6.3.1	Thin Cavities	48
4.6.3.2	Long Cores and Mold Inserts	49
4.7	Fiber-Filled Materials	49
4.7.1	Fiber Concentration	50
4.7.2	Jeffery's Equation	50
4.7.3	A Statistical Approach	51
4.7.4	Mechanical Properties	52
4.8	Shrinkage and Warpage.....	52
4.9	Runners	53

5	Approximations for Injection Molding	55
5.1	Introduction	55
5.2	Material Property Approximations	56
5.3	Filling, Packing, and Cooling Analysis	56
5.3.1	The Thermal Source Term in the Energy Equation	57
5.3.2	Viscosity Modeling	57
5.3.3	Specific Heat Capacity	58
5.3.4	Thermal Conductivity	58
5.3.4.1	Unfilled Amorphous	58
5.3.4.2	Unfilled Semi-Crystalline	59
5.3.4.3	Filled Materials	59
5.3.5	No-Flow or Transition Temperature	59
5.3.6	Pressure-Volume-Temperature (PVT) Data	61
5.3.7	Fiber Orientation, Shrinkage, and Warpage	62
5.3.7.1	Fiber Orientation Analysis	62
5.3.7.2	Shrinkage and Warpage Analysis	63
5.4	Summary of Material Assumptions	63
5.5	Governing Equations	64
5.6	The 2.5D Approximation	65
5.6.1	Governing Equations in Cartesian Coordinates	66
5.6.1.1	Conservation of Mass	66
5.6.1.2	Conservation of Momentum	68
5.6.1.3	Conservation of Energy	68
5.6.2	Estimation of Relevant Terms	69
5.6.3	Velocity in the z Direction	71
5.6.4	Integration of the Momentum Equations	72
5.6.5	Integration of the Continuity Equation	75
5.6.5.1	Summary of the 2.5D Approximation	77
5.7	Mold Cooling Analysis	78
5.8	Fiber Orientation	80
5.8.1	Orientation Tensors	80
5.8.2	Folgar-Tucker Equation	81
5.8.3	Closure Approximations	81
5.8.3.1	Linear Closure	82
5.8.3.2	Quadratic Closure	82
5.8.3.3	Hybrid Closure	82
5.8.3.4	Orthotropic Closure	83
5.8.3.5	The Interaction Coefficient	83

5.9	Shrinkage and Warpage.....	84
5.9.1	Shrinkage Prediction	85
5.9.1.1	Residual Strain Methods	85
5.9.1.2	Residual Stress Models	87
5.10	The 2.5D Approximation for Runners	91
5.10.1	Conservation of Mass for Runners	92
5.10.2	Conservation of Momentum for Runners	93
5.10.3	Conservation of Energy for Runners	93
5.10.4	Integration of the Momentum Equation for Runners	94
5.10.5	Integration of the Continuity Equation for Runners	96
6	Numerical Methods for Solution.....	99
6.1	Midplane Methods	99
6.1.1	Extraction of a Midplane from a 3D Model	100
6.1.2	Dual Domain Analysis for Flow	101
6.1.3	Dual Domain Structural Analysis.....	103
6.1.4	Warpage Analysis Using the Dual Domain FEM.....	107
6.2	3D Analysis	107
6.2.1	Finite Volume Methods	107
6.2.2	A Pseudo-3D Approach	108
6.3	Warpage and Shrinkage Analysis in 3D.....	108
6.4	3D Analysis of Runner Systems	109
II	Improving Molding Simulation	111
7	Improved Fiber Orientation Modeling.....	113
7.1	Introduction.....	113
7.2	ARD Model	114
7.2.1	Evolution Equation	114
7.2.2	Direct Simulation	116
7.2.3	Calculation of C_f	117
7.3	RSC Model	117
7.4	Suspension Rheology	118
7.5	Brownian Dynamics Simulation.....	120

8	Improved Mechanical Property Modeling	123
8.1	Introduction	123
8.2	Unidirectional Composites	124
8.2.1	Effective Stiffness	124
8.2.2	Effective Thermal Expansion Coefficients	126
8.2.3	Effects of Fiber Concentration and Aspect Ratio	126
8.2.3.1	Effect of Fiber Concentration	126
8.2.3.2	Effect of Fiber Aspect Ratio	127
8.3	Fiber Orientation Averaging	130
9	Long Fiber-Filled Materials	131
9.1	Fiber Orientation Evolution Model	131
9.2	Flow-Induced Fiber Migration Model	132
9.3	Fiber Length Attrition Model	134
9.4	Uniaxial Tensile Strength Model	135
9.5	Flexible Fiber Modeling	136
9.5.1	Direct Simulation Methods	136
9.5.2	Continuum Modeling	139
10	Crystallization	141
10.1	Quiescent Crystallization	141
10.1.1	The Kolmogoroff-Avrami-Evans Model	142
10.1.2	The Rate Equations of Schneider	143
10.1.3	Quiescent Nuclei Number Density	144
10.1.4	Growth Rate of Spherulites	145
10.1.5	Material Characterization	146
10.1.5.1	Half-Crystallization Time	146
10.1.5.2	Equilibrium Melting Temperature	146
10.1.5.3	Crystal Growth Rate	148
10.2	Flow-Induced Crystallization	149
10.2.1	Enhanced Nucleation	150
10.2.2	Critical Parameters	151
10.2.3	Shish-Kebab Structure	152
10.2.4	Material Characterization	152
11	Effects of Crystallization on Rheology and Thermal Properties ..	155
11.1	Effects of Crystallization on Rheology	155
11.1.1	Viscosity-Enhancement-Factor Model	155

11.1.2 Two-Phase Model	157
11.2 Effect of Crystallization on PVT	159
11.3 Effect of Crystallization on Specific Heat Capacity	160
11.4 Effect of Crystallization on Thermal Conductivity	161
11.4.1 Non-Fourier Thermal Conduction	161
11.4.2 Van den Brule's Law for Amorphous Polymers	162
11.4.3 Extending the Van den Brule Approach to Semi-Crystalline Polymers.....	162
11.5 Effect of Crystallization on Heat Transfer	164
11.5.1 Stefan's Solution	164
11.5.2 Numerical Solution with Crystallization Kinetics	165
11.6 Modification to the Hele-Shaw Equation	166
12 Colorant Effects.....	167
12.1 Introduction	167
12.2 Material Characterization	168
12.2.1 Morphology	168
12.2.2 Specific Heat	169
12.2.3 Half-Crystallization Time	169
12.2.3.1 Quiescent Crystallization	169
12.2.3.2 Flow-Induced Crystallization.....	169
12.3 Effect on Shrinkage.....	171
13 Prediction of Post-Molding Shrinkage and Warpage	175
13.1 Introduction	175
13.2 Governing Equations.....	176
13.3 Constitutive Equations	177
13.3.1 Viscoelastic Effect.....	177
13.3.2 Thermal Expansion Effect	178
14 Additional Issues of Injection-Molding Simulation.....	181
14.1 Weldlines	181
14.2 Core Shift	182
14.3 Non-Conventional Injection Molds.....	182
14.3.1 Overmolding	182
14.3.2 Gas-Assisted Injection Molding.....	183
14.3.3 Microcellular Injection Foaming Molding	186
14.3.4 Micro-Injection Molding	188
14.4 Viscoelastic Effects	191

14.4.1	Flow-Induced Residual Stress and Birefringence	191
14.4.2	Viscoelastic Instability	193
14.4.3	Viscoelastic Suspensions	194
14.5	Other Numerical Methods	196
14.5.1	Molecular Dynamics Simulation	196
14.5.2	Meshless Methods	197
15	Epilogue	201
Appendices		203
A	History of Injection-Molding Simulation	205
A.1	Early Academic Work on Simulation	205
A.2	Early Commercial Simulation	206
A.3	Simulation in the Eighties	208
A.3.1	Academic Work in the Eighties	209
A.3.1.1	Mold Filling	209
A.3.1.2	Mold Cooling	211
A.3.1.3	Warpage Analysis	212
A.3.2	Commercial Simulation in the Eighties	212
A.3.2.1	Codes Developed by Large Industrials and Not for Sale	214
A.3.2.2	Codes Developed by Large Industrials for Sale in the Marketplace	214
A.3.2.3	Companies Devoted to Developing and Selling Simulation Codes	215
A.4	Simulation in the Nineties	216
A.4.1	Academic Work in the Nineties	217
A.4.2	Commercial Developments in the Nineties	218
A.4.2.1	SDRC	218
A.4.2.2	Moldflow	219
A.4.2.3	AC Technology/C-MOLD	220
A.4.2.4	Simcon	220
A.4.2.5	Sigma Engineering	220
A.4.2.6	Timon	221
A.4.2.7	Transvalor	221
A.4.2.8	CoreTech Systems	221
A.5	Simulation Science Since 2000	221
A.5.1	Commercial Developments Since 2000	223
A.5.1.1	Moldflow	224
A.5.1.2	Timon	225

A.5.1.3 CoreTech Systems	225
A.5.1.4 Autodesk.....	225
A.5.2 Note for Students	225
B Tensor Notation	227
B.1 Index Notation	227
B.2 Einstein Summation Convention	228
B.3 Kronecker Delta.....	229
B.4 Alternating Tensor	229
B.5 Product Operations of Two Tensors	230
B.6 Transpose Operation	230
B.7 Transformation of Principal Axes	231
B.8 Gradient of a Field	233
B.9 Unit Vector \mathbf{p} and Operator $\partial/\partial\mathbf{p}$	233
B.10 Identities	234
C Derivation of Fiber Evolution Equations	235
C.1 The Langevin Equation	235
C.2 Probability Density Function and Orientation Tensors	237
C.3 Equations of Change for the Orientation Tensors.....	238
C.3.1 Isotropic Rotary Diffusion Model (Folgar-Tucker Model)	239
C.3.2 Anisotropic Rotary Diffusion Model	241
D Dimensional Analysis of Governing Equations	243
D.1 Conservation of Mass	244
D.2 Conservation of Momentum	245
D.3 The Energy Equation	248
D.4 Summary	250
D.4.1 Conservation of Mass	250
D.4.2 Conservation of Momentum	250
D.4.3 Energy Equation	251
E The Finite Difference Method	253
E.1 Introduction to the Finite Difference Method	253
E.1.1 A Simple Example	255
E.2 Application to Temperature Calculation	257
E.2.1 Explicit Methods	257
E.2.1.1 Stability Criteria for Explicit Methods	258
E.2.2 Implicit Methods.....	258

F	The Finite Element Method	261
E1	Basic Terminology	261
E2	The Finite Element Approach	262
E2.1	Geometric Modeling of the Solution Domain	262
E2.2	Meshing	263
E2.3	Derivation of Element Equations	263
E2.4	Assembly of Element Equations	263
E2.5	Application of Boundary Conditions	264
E2.6	Solution of the System Equations	264
E2.7	Display of Results	264
E3	The Nature of a Finite Element Solution	265
E4	Shape Functions	267
E5	Approximating Nodal Values	267
E5.1	Weighted Residual Methods	268
E6	Constraint Equations	268
E6.1	Special Case 1: Two Unknowns Equal	271
E6.2	Special Case 2: One Known Constraint	272
E7	A One-Dimensional Problem Solved Using the FEM	273
E7.1	Meshing	273
E7.2	Derivation of Element Equations	274
E7.3	Assembly	278
E7.4	Application of Boundary Conditions	280
E7.5	Solution of System Equations	281
G	Numerical Methods for the 2.5D Approximation	283
G.1	Overview of Solution Process	283
G.1.1	Numerical Methods	284
G.2	Finite Element Formulation for the Pressure Field	285
G.2.1	Interpolation Functions	285
G.2.2	Area Coordinates	286
G.3	Finite Element Derivation	287
G.3.1	Assembly of Element Equations and Solution	295
G.4	Solution of the Energy Equation	296
G.4.1	Finite Difference Discretization	296
G.4.2	Solution of the Conduction Problem	297
G.4.3	Explicit Method	297
G.5	Flow Front Advancement	298
G.6	Runners	298

H	Three-Dimensional FEM for Mold Filling Analysis	303
	H.1 Governing Equations.....	303
	H.2 Weak Formulations.....	304
	H.3 Finite Element Matrix Formulations.....	305
	H.4 Solution Procedures.....	309
	H.5 Flow-Front Advancement	310
	H.6 Numerical Solution For Temperature Field	311
I	Level Set Method	313
J	Full Form of Mori-Tanaka Model	317
	J.1 Eshelby Tensor Components.....	317
	J.1.1 Material with Isotropic Matrix and Inclusions.....	317
	J.1.2 General Anisotropic Materials	318
	J.2 Expanded Mori-Tanaka Equation	319
	J.2.1 Contracted Notation for Stiffness Tensor and Compliance Tensor	319
	J.2.2 Inverse of a Matrix	319
	J.2.3 Expanded Expression of the Mori-Tanaka Equation	320
	Bibliography	321
	Index	345