

Antoni Ligęza

Logical Foundations for Rule-Based Systems

Studies in Computational Intelligence, Volume 11

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ISBN 3-540-29117-2

Antoni Ligeza

Logical Foundations for Rule-Based Systems

Second Edition



Springer

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Library of Congress Control Number: 2005932569

Originally published in Poland by AGH University of Science and Technology Press, Kraków, Poland

ISSN print edition: 1860-949X

ISSN electronic edition: 1860-9503

ISBN-10 3-540-29117-2 Springer Berlin Heidelberg New York

ISBN-13 978-3-540-29117-6 Springer Berlin Heidelberg New York

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Printed in The Netherlands

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Typesetting: by the author and TechBooks using a Springer L^AT_EX macro package

Printed on acid-free paper SPIN: 11506492 89/TechBooks 54321

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